



Mark Scheme (Results)

Summer 2024

Pearson Edexcel International Advanced Level
In Statistics S2 (WST02) Paper 01

Question	Scheme		Marks
1(a)	The random variable M is such that $M \sim \text{Po}(2)$		
(i)	$[P(M \leq 3)] = 0.8571$	awrt 0.857	B1
(ii)	$P(M \leq 6) = 1 - P(M \leq 5)$		M1
	$= 0.0166$ (calc 0.016563...)	awrt 0.0166	A1
			(3)
(b)	$Q \sim \text{Po}(6)$		M1
	$P(4 \leq Q \leq 7) = P(Q \leq 7) - P(Q \leq 3) [= 0.5928]$		M1
	$X \sim \text{B}(20, "0.5928")$ and $P(X = 15)$ or ${}^{20}C_{15} ("0.5928")^{15} (1 - "0.5928")^5$		M1
	$= 0.06809...$	awrt 0.068	A1
			(4)
(c)	$H_0: \lambda = 2 \quad H_1: \lambda > 2$		B1
	$R \sim \text{Po}(5) : P(R \leq 10)$ or $1 - P(R \leq 9)$		M1
	$= 0.0318$	or CR: $R \leq 10$	A1
	Reject H_0 or Significant or in the critical region		M1
	There is evidence to support the manager's belief / rate of customers arriving at the garage has increased		A1
			(5)
(d)	The number of tyres bought is likely not to occur singly/tyres are not sold independently.		B1
			(1)
Notes			Total 13
(a)	B1	awrt 0.857	
	M1	for $1 - P(M \leq 5)$ or $1 - 0.9834$ Do not allow $1 - P(M < 6)$ unless $1 - P(M \leq 5)$ is used	
	A1	awrt 0.0166 correct answer scores 2 out of 2	
(b)	M1	for writing or using $\text{Po}(6)$	
	M1	for $P(Q \leq 7) - P(Q \leq 3)$ or $0.7440 - 0.1512$ or awrt 0.593	
	M1	For $\text{B}(20, "0.5928")$ and $P(X = 15)$ or ${}^{20}C_{15} (p)^{15} (1 - p)^5$ (implied by awrt 0.068)	
	A1	awrt 0.068	
(c)	B1	for correct hypotheses in terms of λ or μ Allow 5 instead of 2. These must be attached to H_0 and H_1 correctly	
	M1	for writing or using $\text{Po}(5)$ and $P(R \leq 10)$ or $1 - P(R \leq 9)$ (may be implied by awrt 0.0318 or correct CR)	
	A1	awrt 0.0318 allow CR: $[R] \leq 10$ allow any letter or no letter for CR	
	M1	for a correct ft statement consistent with their p -value and 0.05 or with 10 and their CR Need not be contextual but there must be no contradicting non-contextual comments	
	A1	dep on 1 st and 2 nd M1 for a correct conclusion in context which must be rejecting H_0 Must use bold words (oe)	
(d)	B1	for the idea that tyres may be bought in e.g. pairs oe/the idea that tyre sales are not independent	

Question	Scheme		Marks
2(a)	$\frac{3}{10}d - \frac{1}{75}d^2 - \frac{2}{3} = 1$		M1
	$45d - 2d^2 - 100 = 150$ or $\frac{3}{10}d - \frac{1}{75}d^2 - \frac{5}{3} = 0 \rightarrow 2d^2 - 45d + 250 = 0^*$		A1*
			(2)
(b)	$P(1 < H < 4.5) = \left(\frac{4.5}{6} - \frac{1}{3}\right) - \left(\frac{1}{48}\right) = \frac{19}{48}$ or 0.39583...		M1
	$P(1 < H < 1.5) = \left(\frac{1.5^2}{48}\right) - \left(\frac{1}{48}\right) = \frac{5}{192}$ or 0.02604...		M1
	$P(H < 1.5 1 < H < 4.5) = \frac{"0.02604..."}{"0.3958..."} = \frac{5}{76}$ or 0.06578... awrt 0.0658		M1 A1
			(4)
	(c)	$[f(h) =] \begin{cases} \frac{h}{24} & 0 < h, 4 \\ \frac{1}{6} & 4 < h, 5 \\ \frac{3}{10} - \frac{2}{75}h & 5 < h, d \\ 0 & otherwise \end{cases}$	M1 M1 A1
			(3)
Notes			Total 9
(a)	M1	for $\frac{3}{10}d - \frac{1}{75}d^2 - \frac{2}{3} = 1$	
	A1*	cso at least one step seen before given answer e.g. removing the denominator or correct 3 term quadratic = 0	
(b)	M1	correct method to find $P(1 < H < 4.5)$ implied by $\frac{19}{48}$ or awrt 0.396	
	M1	for writing or finding $P(1 < H < 1.5)$ implied by $\frac{5}{192}$ or awrt 0.026	
	M1	for $\frac{p}{"0.3958"}$ where $0 < p < "0.3958"$	
	A1	awrt 0.0658	
(c)	M1	for one of row 1, 2 or 3 correct. Allow any letters. Condone missing/incorrect range	
	M1	for any two rows correct with ranges. Allow any letters and < for ,, signs	
	A1	Fully correct. all the same letter in rows 1 to 3 Allow < for ,, signs condone $d = 10$ but not $d = 12.5$	

Question	Scheme		Marks
3(a)	A list of all the shops		B1
			(1)
(b)	The shops		B1
			(1)
(c)	Advantage - A sample is quicker/ cheaper / easier to process		B1
	Disadvantage – less accurate/ may be biased / may not be representative		B1
			(2)
(d)	P($X \leq 6$) = 0.0172 <u>or</u> P($X \leq 18$) = 0.0212 <u>or</u> P($X \leq 17$) = 0.9788 <u>or</u> $X \leq 6$ <u>or</u> $X \leq 18$		M1
	$[P(X \leq 6)] = 0.0172$ and $[P(X \leq 18)] = 0.0212$		A1
	CR: $[0,]X \leq 6, 18, X \leq 30]$		A1
			(3)
(e)	20 is in the critical region therefore there is evidence that Jian's belief is incorrect		B1ft
			(1)
(f)	$H_0 : p = 0.4 \quad H_1 : p < 0.4$		B1
	$J \sim B(150, 0.4) \Rightarrow \approx N(60, 36)$		M1A1
	$P(J \leq 47) \approx P\left(Z \leq \frac{47.5 - 60}{6} [= -2.08333...]\right)$		M1
	$= 0.0188$ (calc 0.018610...)		M1
	CR: $J < \text{awrt } 49.6$		A1
	There is sufficient evidence to suggest that the proportion of shops where the stocktaking system is being used incorrectly is less than 0.4/decreased		A1
			(7)
Notes			Total 15
(a)	B1	for the idea of a list/database(oe) of all shops list of all stocktaking systems is B0	
(b)	B1	for allow shop or store(s) the number of shops is B0 the stocktaking systems at each shop is B0	
(c)	B1	for a correct advantage for a sample oe eg allow census take longer than a sample e.g. 'a sample is more uncertain' on its own is B0	
	B1	for a correct disadvantage for a sample oe eg a census is more accurate than a sample	
		If there is no reference to sample or census assume referring to sample. Ignore extraneous non-contradictory comments	
(d)	M1	for one of these probability statements correct <u>or</u> awrt 0.017 <u>or</u> awrt 0.021 <u>or</u> awrt 0.98 <u>or</u> one correct CR	
	A1	for both probabilities awrt 0.0172 and awrt 0.0212	
	A1	for both CR correct oe e.g. $X < 7, X > 17$ ignore any symbol used between the two CR tails allow any or no letter (do not allow CR stated as probabilities)	
(e)	B1ft	for stating 20 is in the CR and give correct statement. Allow the belief in words. Only ft if their CR is in the form $X \leq C_1 \cup X \leq C_2$ (allow as probability statements)	
(f)	B1	for both hypotheses correct, using p or π . Must be attached to H_0 and H_1	
	M1	for writing or using $N(60, \dots)$	
	A1	for writing or using $N(60, 36)$	
	M1	for standardising (allow \pm) using their "60" and "6" with either 46.5, 47 or 47.5 for CR method $n, n + 0.5$ or $n - 0.5$ and equate to -1.6449 or better	
	M1	for using the correct continuity correction 47.5 or $(n + 0.5)$	
	A1	for awrt 0.019 <u>or</u> CR: $J < \text{awrt } 49.6$ or $J + 0.5 < \text{awrt } 50.1$ Exact binomial gives 0.01756...and scores M0A0M0M0A0	
	A1	dep on previous A1 for a correct conclusion in context using bold word (oe) Do not allow 'number' for 'proportion'	

Question	Scheme		Marks																	
4(a)	$\frac{10}{50} \times \frac{9}{49} \left[= \frac{9}{245} * \right]$		B1cso (1)																	
(b)	number of counters numbered 4 = 10 numbered 7 = 15 numbered 10 = 25 $M = 4, 5.5, 7, 8.5, 10$		M1 B1																	
	$P(M = 5.5) = 2 \times \frac{10}{50} \times \frac{15}{49} \left[= \frac{6}{49} \right]$		M1																	
	$P(M = 7) = 2 \times \frac{10}{50} \times \frac{25}{49} + \frac{15}{50} \times \frac{14}{49} \left[= \frac{71}{245} \right]$		M1																	
	$P(M = 8.5) = 2 \times \frac{15}{50} \times \frac{25}{49} \left[= \frac{15}{49} \right]$		M1																	
	$P(M = 10) = \frac{25}{50} \times \frac{24}{49} \left[= \frac{12}{49} \right]$																			
	<table border="1" style="width: 100%; text-align: center;"> <thead> <tr> <th>m</th> <th>4</th> <th>5.5</th> <th>7</th> <th>8.5</th> <th>10</th> </tr> </thead> <tbody> <tr> <td>$P(M = m)$</td> <td>$\frac{9}{245}$</td> <td>$\frac{6}{49}$</td> <td>$\frac{71}{245}$</td> <td>$\frac{15}{49}$</td> <td>$\frac{12}{49}$</td> </tr> <tr> <td></td> <td>(awrt) 0.037</td> <td>(awrt) 0.122</td> <td>(awrt) 0.290</td> <td>(awrt) 0.306</td> <td>(awrt) 0.245</td> </tr> </tbody> </table>		m	4	5.5	7	8.5	10	$P(M = m)$	$\frac{9}{245}$	$\frac{6}{49}$	$\frac{71}{245}$	$\frac{15}{49}$	$\frac{12}{49}$		(awrt) 0.037	(awrt) 0.122	(awrt) 0.290	(awrt) 0.306	(awrt) 0.245
m	4	5.5	7	8.5	10															
$P(M = m)$	$\frac{9}{245}$	$\frac{6}{49}$	$\frac{71}{245}$	$\frac{15}{49}$	$\frac{12}{49}$															
	(awrt) 0.037	(awrt) 0.122	(awrt) 0.290	(awrt) 0.306	(awrt) 0.245															
			(6)																	
(c)	$\left(1 - \frac{9}{245}\right)^n < 0.15$		M1																	
	$n = 50.689... \text{ or } n = 50 \text{ is } 0.1539... \text{ or } n = 51 \text{ is } 0.148... \text{ or } [n >] \frac{\log 0.15}{\log(1 - \frac{9}{245})}$		M1																	
	$n = 51$		A1																	
			(3)																	
Notes			Total 10																	
(a)	B1	A correct equivalent expression																		
(b)	M1	For 10, 15 and 25 - may be seen in (a) or may be seen in probability expressions																		
	B1	all means correct with no incorrect extra unless they have a probability of 0																		
	M1	One correct probability (not including 9/245)																		
	M1	Two correct probabilities (not including 9/245)																		
	M1	Three correct probabilities (not including 9/245)																		
	A1	fully correct. need not be in a table but must have correct probability associated with correct mean																		
	SC	With replacement using probabilities $\frac{10}{50}, \frac{15}{50}, \frac{25}{50}$ gives $\frac{3}{25}, \frac{29}{100}, \frac{3}{10}, \frac{1}{4}$ can score maximum M1B1M1(two correct)M1(four correct)M0A0																		
(c)	M1	Setting up a correct inequality (allow any inequality or equal sign here)																		
	M1	for a value $n = \text{awrt } 50.7 \text{ or } \text{awrt } 0.154 \text{ or } \text{awrt } 0.148$ or correct log expression for n																		
	A1	51 cao do not allow $n \dots 51$																		

Question	Scheme		Marks
5(a)	$D \sim B(8, 0.05)$		M1
	$P(D \dots 2) = 1 - P(D, , 1)$		M1
	$= 0.0572$ (calc 0.057244...) awrt 0.0572		A1
			(3)
(b)	$E \sim Po(50)$		M1
	$P(E = 45) = \frac{e^{-50} \times 50^{45}}{45!}$		M1
	$= 0.0458262\dots$ awrt 0.0458		A1
			(3)
(c)	$P(T > 16) = \frac{50-16}{50-10}$ or $1 - \frac{16-10}{50-10}$		M1
	$= 0.85$		A1
			(2)
(d)	$P(T < 40) = 0.75$		M1
	$F =$ number of customers ringing in the next 40 seconds has $F \sim Po(4)$		
	$P(F = 0) [= e^{-4} =$ awrt 0.0183]		M1
	$P(\text{Jia reaches the correct department and } F = 0) = 0.75 \times 0.95 \times e^{-4}$		dM1
	$= 0.013049\dots$ awrt 0.013		A1
		(4)	
Notes			Total 12
(a)	M1	for writing or using $B(8, 0.05)$	
	M1	for writing or using $1 - P(D, , 1)$	
	A1	awrt 0.0572	
(b)	M1	for writing or using $Po(50)$	
	M1	for $\frac{e^{-\lambda} \times \lambda^{45}}{45!}$ with any value of λ (may be implied by awrt 0.046)	
	A1	awrt 0.0458	
(c)	M1	for a correct method to find $P(T > 16)$	
	A1	for 0.85 oe correct answer scores 2 out of 2	
(d)	M1	for 0.75 oe	
	M1	for attempting $P(F = 0)$ from $Po(\lambda)$ allow any λ	
	dM1	dep on previous M1 "0.75" \times 0.95 \times "e ⁻⁴ "	
	A1	awrt 0.013	

Question	Scheme	Marks	
6(a)	$\int_{-1}^3 (a+bx) dx [=1]$ <u>or</u> trapezium drawn	M1	
	$\left[ax + \frac{bx^2}{2} \right]_{-1}^3 [=1]$ oe <u>or</u> $\frac{3-(-1)}{2} ((a-b) + (a+3b)) [=1]$	A1	
	$\left[3a + \frac{9b}{2} \right] - \left[-a + \frac{b}{2} \right] = 1$ oe <u>or</u> $\frac{4}{2}(2a+2b) = 1 \Rightarrow 4a+4b = 1^*$	A1*	
		(3)	
(b)(i)	$\int_{-1}^3 ax^2 + bx^3 dx = \left[\frac{ax^3}{3} + \frac{bx^4}{4} \right]_{-1}^3$	M1A1	
	$\left[\frac{27a}{3} + \frac{81b}{4} \right] - \left[-\frac{a}{3} + \frac{b}{4} \right] = \frac{17}{5}$	dM1	
	$\frac{28}{3}a + 20\left(\frac{1-4a}{4}\right) = \frac{17}{5}$	M1 A1	
		(5)	
(ii)	$-\frac{32}{3}a = -\frac{8}{5}$ oe <u>or</u> $\frac{28}{3}\left(\frac{1-4b}{4}\right) + 20b = \frac{17}{5}$	M1	
	$b = \frac{1-4 \times 0.15}{4} \Rightarrow b = 0.1^*$	A1*	
		(2)	
(c)		M1 A1	
		(2)	
(d)	$\left["0.15" k + \frac{0.1k^2}{2} \right] - \left[-"0.15" + \frac{0.1}{2} \right] = 0.2$ <u>or</u> $\frac{1}{2}(k+1)(0.05+0.1k+0.15) = 0.2$	$\left[0.45 + \frac{0.9}{2} \right] - \left["0.15" k + \frac{0.1k^2}{2} \right] = 0.8$ <u>or</u> $\frac{1}{2}(3-k)(0.15+0.1k+0.45) = 0.8$	M1
	$0.05k^2 + 0.15k - 0.1 = 0$	A1	
	$k = \frac{-0.15 \pm \sqrt{0.15^2 - 4 \times 0.05 \times (-0.1)}}{2 \times 0.05}$	M1	
	$= 0.56155\dots$ awrt 0.562	A1	
		(4)	
		Total 16	

		Notes
(a)	M1	for an attempt to integrate $a + bx$ with either $a \rightarrow ax$ or $x \rightarrow x^2$ ignore limits or for trapezium drawn with parallel sides correct in terms of a and b (may be implied by correct area of trapezium)
	A1	correct integration or correct area of trapezium
	A1*	cso (correct limits seen substituted or correct area) equated to 1 which leads to final given answer
		Mark b(i) and b(ii) together
(b)(i)	M1	for an attempt to integrate $ax^2 + bx^3$ with either $x^2 \rightarrow x^3$ or $x^3 \rightarrow x^4$ ignore limits
	A1	correct integration ignore limits
	dM1	dep on previous M1. Substituting in correct limits and equating to 17/5
	M1	substituting $4b = 1 - 4a$ oe
	A1	a correct equation
(ii)	M1	solving their equation in a in the form $na = c$ where $n \neq 1$ or a correct equation in terms of b M0 for $a = 0.15$ without working or for using $b = 0.1$ in $4a + 4b = 1$ to find a
	A1*	for a correct un-simplified expression for b leading to given answer $b = 0.1$ * which must come from correct working
(c)	M1	correct shape (straight line with positive gradient) must be above x -axis and must be between -1 and 3 ignore graph before -1 and after 3
	A1	correct with both correct x -axis labels -1 and 3 and at least 1 correct y -axis label from $0.05, 0.15$ or 0.45 ignore graph before -1 and after 3
(d)	M1	for a correct equation using integration or area need not be simplified. use of limit $k + 1$ instead of k in integration is M0
	A1	correct 3 term quadratic (oe)
	M1	correct method seen to solve their 3 term quadratic or awrt 0.562 or awrt -3.56
	A1	awrt 0.562 with other solutions eliminated if given Allow $\frac{\sqrt{17} - 3}{2}$